Programm	BS Computational Statistics and Data Analytics	Course Code	CSTA-301	Credit Hours	3				
	Multivariate Analysis								
	Course Introduction								
This course introduces the theory and applications of multivariate statistical methods. It focuses on techniques used to analyze data consisting of multiple variables, exploring how these variables interrelate. Topics include multivariate normal distribution, hypothesis testing, principal component analysis, factor analysis, discriminant analysis, and cluster analysis.									
Learning Outcomes									
<ul> <li>By the end of this course, students will be able to:</li> <li>1. Understand and apply multivariate statistical methods.</li> <li>2. Analyze multivariate data and interpret the results.</li> <li>3. Use statistical software to perform multivariate analyses.</li> <li>4. Develop skills to critically evaluate multivariate analyses in research.</li> </ul>									
	Course Conten	nt		Assignmen gs	ts/Readin				
Unit – I         Definition and scope of multivariate analysis.         Week 1       Refreshing fundamental concepts in matrix algebra: matrices, vectors, operations (addition, subtraction, multiplication), and properties         Unit – II         Encoded of the function of the late			ebra: matrices, plication), and						
Week 2       Unit – III         Multivariate Distributions:         Introduction to multivariate distributions and their significance in statistical modeling         Unit – IV         Overview of probability density functions for multivariate data									
Week 3       Unit – V         Week 3       Understanding the concept of multivariate distributions and their characteristics         Unit – VI       Exploration of joint probability distributions for multiple random variables									
Week 4	Week 4       Unit – VII         The Multivariate Normal Distribution:         Detailed study of the multivariate normal distribution as a fundamental distribution in multivariate analysis								

	Unit – VIII		
	Properties and characteristics of the multivariate normal distribution		
	Unit – IX		
Week 5	Multivariate Normal Distribution Properties:		
	Advanced properties of the multivariate normal distribution: mean, variance, covariance, and correlation		
	Unit – X		
	Understanding the implications of multivariate normality in statistical		
	analysis		
	Unit – XI		
	Estimation of the Mean Vector:		
Week 6	Techniques for estimating the mean vector of multivariate data samples		
	Unit – XII		
	Understanding the properties and limitations of mean vector estimation methods		
	Unit – XIII		
	The Covariance Matrix:		
Week 7	Understanding the covariance matrix and its role in describing the		
	relationships between variables in multivariate data		
	Unit – XIV		
	Properties and interpretations of the covariance matrix		
	Unit – XV		
	Conditional Distribution of M.V normal		
Week 8	Mean and variance of conditional Distribution		
	Unit –XVI		
	Hotelling's T^2 test		
	Inferences for Multivariate Means		
Week 9	Confidence regions for multivariate means.		
	Unit – XVIII		
	Practical Application of mean vectors inferences		
	Eactor Analysis		
Week 10	Exploratory factor analysis, model specification, and identification.		
	Unit – XX		
	Confirmatory factor analysis, rotations in factor analysis, and interpretation of factors.		
	Unit – XXI		
	Canonical Correlation Analysis (CCA)		
Week 11	Concept of canonical variables, estimation and interpretation.		
	Unit – XXII		
	Practical applications of CCA and case studies.		

	Unit – XXIII		
Week 12	Discriminant Analysis		
	linear Discriminant Analysis		
	Unit – XXIV		
	Quadratic Discriminant Analysis		
	Unit – XXV		
	Principal Component Analysis (PCA)		
Week 13	The concept and objectives of PCA,		
	Unit – XXVI		
	Eigenvalues and eigenvectors.		
Week 14	Unit – XXVII		
	Application of PCA		
	Interpreting principal components, applications		
	Unit – XXVIII		
	Dimension Reduction		
	Use of PCA in dimensionality reduction.		
	Unit – XXIX		
Week 15	Cluster Analysis		
	Hierarchical Clustering		
	Unit – XXX K means clustering		
Week 16	Init – XXXI		
	Optimum number of clustering		
	Unit – XXXII		
	Overview and summary		
Textbooks and Reading Material			

## **Text Book**

1. Johnson, R.A., & Wichern, D.W. (2008). *Applied multivariate statistical analysis*. Pearson Education: Singapore.

## **Suggested Readings**

1. Anderson, T.W. (2003). An introduction to multivariate statistical analysis (3rd ed.). John Wiley & Sons: New York.

2. Chatfield, C., & Collins, A.J. (1981). Introduction to multivariate analysis. Chapman and Hall: London.

3. Morrison, D.F. (2004). *Multivariate statistical methods* (4<sup>th</sup> ed.). McGraw Hill Publishing Co, New York.

## **Teaching Learning Strategies**

Class Lecture method, which includes seminars, discussions, assignments and projects. (Audio-visual tools are used where necessary)

## Assignments: Types and Number with Calendar

According to the choice of respective teacher.

Assessment					
Sr. No.	Elements	Weightage	tage Details		
1.	Midterm Assessment	35%	It takes place at the mid-point of the semester.		
2.	Formative Assessment	25%	It is continuous assessment. It includes: Classroom participation, attendance, assignments, and presentations, homework, attitude and behavior, hands-on-activities, short tests, quizzes etc.		
3.	Final Assessment	40%	It takes place at the end of the semester. It is mostly in the form of a test, but owing to the nature of the course the teacher may assess their students based on term paper, research proposal development, field work and report writing etc.		